

# KS2 Maths

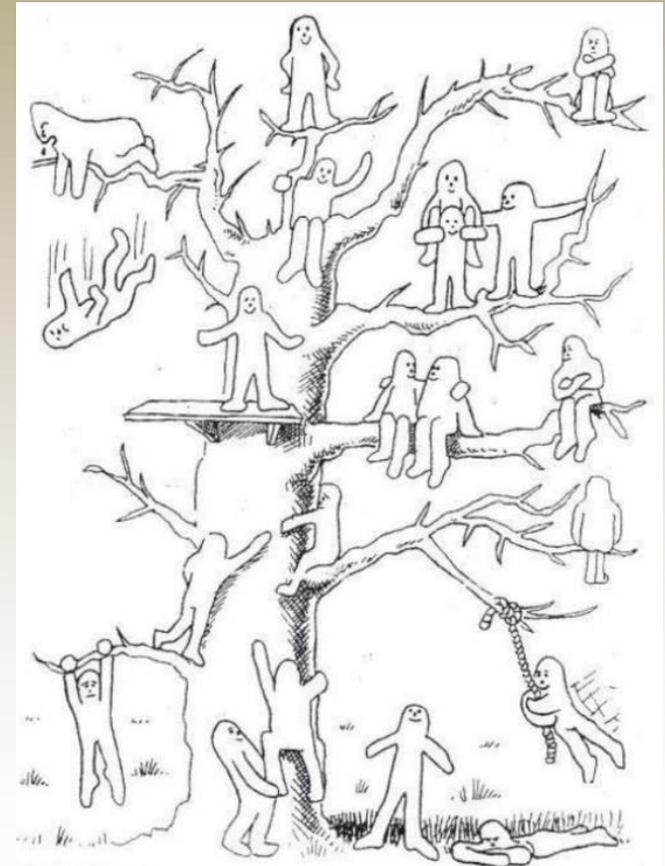
Tuesday 3<sup>rd</sup> December 2024



Look at the picture of the Blob Tree.

When it comes to maths, which Blob represents you the best and why?

Which Blob do you think represents your child?



# Agenda



1. Calculation policy
2. Mathematical language
3. Practical resources and visual representations

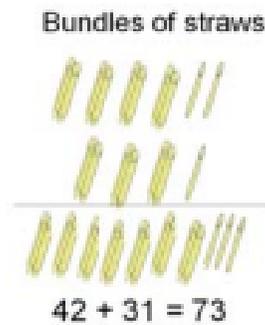




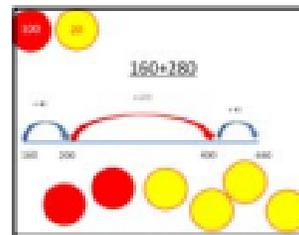
# Calculation policy

Representations to support mental and written calculations.

Use a range of concrete, pictorial and abstract representations, including those below



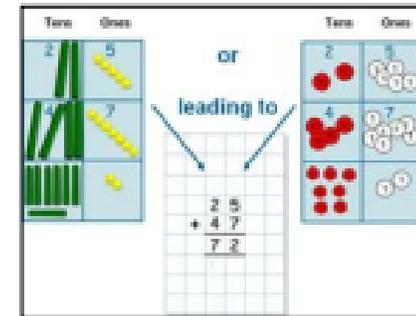
$$\begin{array}{l} 0 + 50 + 3 \\ 10 + 40 + 3 \\ 20 + 30 + 3 \\ 30 + 20 + 3 \\ 40 + 10 + 3 \\ 50 + 0 + 3 \end{array}$$



$$\begin{array}{r} 76 + 21 \\ = 70 + 6 + 20 + 1 \\ = 90 + 7 = 97 \end{array}$$

What is the same and what is different about all these methods?

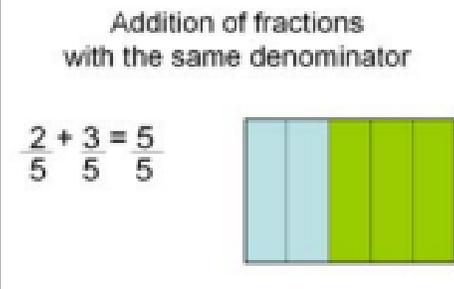
I can explain my method using representations



Dienes and place value counters

Fractions

Addition of fractions with the same denominator within one whole.





# Calculation policy

Written  
Calculations

**Add numbers with up to three digits, using formal written (columnar) methods**

Add to three digit numbers using physical and abstract representations (e.g. straws, dienes, place value counters, empty number lines)

- Straws, dienes, place value counters, empty number lines

$30 + 4$	$\rightarrow$	$34$
$20 + 5$		$+25$
<hr/>		<hr/>
$50 + 9$		$59$

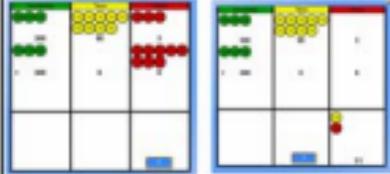
$200 + 30 + 4$		$234$
$500 + 20 + 7$	$\rightarrow$	$+ 527$
<hr/>		<hr/>
$700 + 60 + 1$		$761$
$10$		$1$

**Revert to concrete representations if children find expanded/column methods difficult**





# Calculation policy

<p>Written Calculations</p>	<p><b>Add whole numbers with more than four digits, using the formal written (columnar) method</b></p> <p>Add three digit numbers using columnar method and then move onto 4 digits. Include decimal addition for money</p> <div style="display: flex; justify-content: space-around;"><div style="border: 1px solid black; padding: 5px;"><math display="block">\begin{array}{r} 24172\text{m} \\ + 5929\text{m} \\ \hline 30101\text{m} \\ \hline 1111 \end{array}</math></div><div style="border: 1px solid black; padding: 5px;"><math display="block">\begin{array}{r} \text{£}563.14 \\ + \text{£}207.88 \\ \hline \text{£}771.02 \\ \hline 111 \end{array}</math></div></div> <p style="text-align: center; background-color: orange; padding: 5px;"><b>Revert to expanded methods if children find formal calculation method difficult (see Y3)</b></p>
<p>Representations to support mental and written calculations.</p>	<p><b>Use physical/pictorial representations alongside columnar methods where needed.</b></p> <div style="display: flex; justify-content: space-between;"><div style="border: 1px solid black; padding: 5px;"><math display="block">\begin{aligned} 12\ 462 + 2300 \\ = 12\ 462 + 2000 + 300 \\ = 14\ 462 + 300 \\ = 14\ 762 \end{aligned}</math><p style="text-align: center;">Partitioning and recombining</p></div><div style="text-align: center;"><p>Ask what is the same and what is different about all these methods?</p><p>Jottings to support mental calculation</p></div><div style="border: 1px solid black; padding: 5px;"><p>Place Value counters to support column addition</p><math display="block">\begin{array}{r} 393 \\ + 308 \\ \hline 1 \\ \hline 1 \end{array}</math></div></div>



# Calculation policy

Written  
Calculations

**Add and subtract whole numbers with more than 4 digits, including using formal written methods (columnar addition and subtraction).**

***(Pupils) practise adding and subtracting decimals.***

Begin with three-digit numbers using formal, columnar method; then move into four-digit numbers.

As in Year 4, compare physical and / or pictorial representations and expanded algorithms alongside columnar methods. Ask: *What is the same? What's different?*

Compare and discuss the suitability of different methods, (mental or written), in context.

Revert to expanded methods whenever difficulties arise

£17.34—£12.16

$$\begin{array}{r} 1000+700+20+14\text{p} \\ -1000+200+10+6\text{p} \\ \hline 500+10+8\text{p} \end{array}$$



$$\begin{array}{r} 2 \\ 1734\text{p} \\ -1216\text{p} \\ \hline 518\text{p} \end{array}$$



$$\begin{array}{r} \text{£ } 2 \\ 17.34 \\ -12.16 \\ \hline 5.18 \end{array}$$

*What is the same  
about these models?  
What's different?*

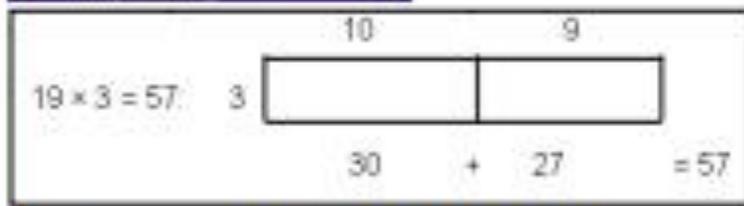
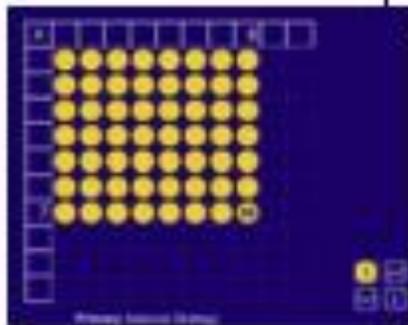
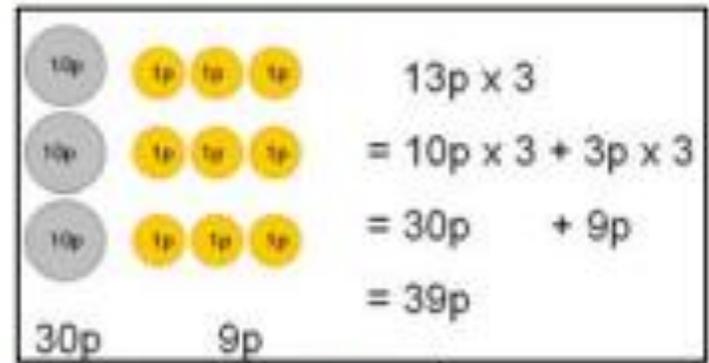
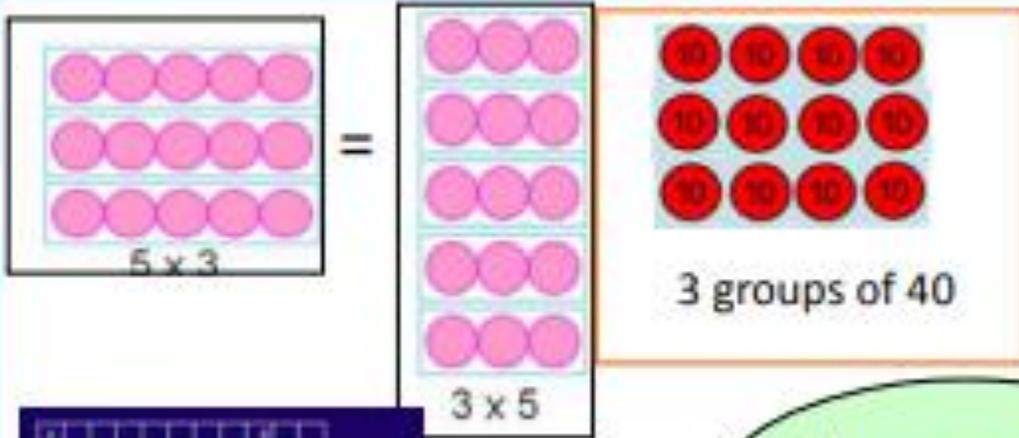
Relate place value of decimals with that of whole numbers using representations. See below.





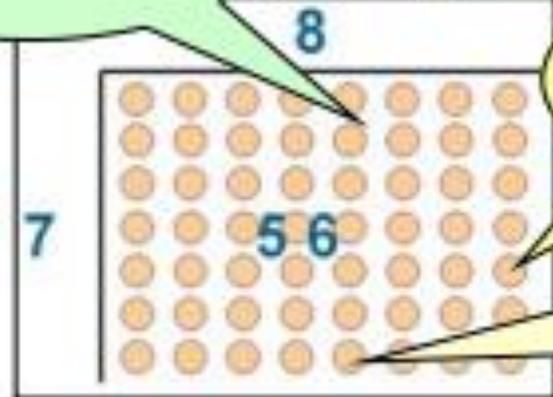
# Calculation policy

Representations to support mental and written calculations.



Use arrays for partitioning too

I can see eight groups of seven!



I can see seven, eight times!

And seven groups of eight!



# Calculation policy

- multiply numbers up to 4 digits by a one- or two-digit number using a formal written method, including long multiplication for two-digit numbers

Written  
Calculations

24 × 16 becomes

$$\begin{array}{r} 24 \\ \times 16 \\ \hline 144 \\ 240 \\ \hline 384 \end{array}$$

124 × 26 becomes

$$\begin{array}{r} 124 \\ \times 26 \\ \hline 744 \\ 2480 \\ \hline 3224 \end{array}$$

Answer: 3224

124 × 26 becomes

$$\begin{array}{r} 124 \\ \times 26 \\ \hline 744 \\ 2480 \\ \hline 3224 \end{array}$$

Answer: 3224

2741 × 6 becomes

$$\begin{array}{r} 2741 \\ \times 6 \\ \hline 16446 \end{array}$$

Answer: 16 446

Compact methods for multiplication are efficient but often do not make the value of each digit explicit. When introducing multiplication of decimals, it is sensible to take children back to an expanded form such as the grid method where the value of each digit is clear, to ensure that children understand the process.

Does your answer seem reasonable?

**Revert to expanded methods if children find formal calculation method difficult (see Y3/Y4)**





# Calculation policy

<p>Written Calculations</p>	<p><b>Pupils should be taught to:</b></p> <ul style="list-style-type: none"> <li>•write and calculate mathematical statements for multiplication and division using the multiplication tables that they know, including for two-digit numbers times one-digit numbers, using mental and progressing to formal written methods.</li> <li>•solve problems, including missing number problems, involving multiplication and division, including positive integer scaling problems and correspondence problems in which n objects are connected to m objects, (see <u>Links from other strands</u>, below.)</li> </ul> <div style="border: 1px solid gray; padding: 5px; margin: 10px 0;"> <p>"I know <math>6 \div 3 = 2</math>, so <math>60 \div 3 = 20</math>."              "I know <math>12 \div 3 = 4</math>, so <math>120 \div 3 = 40</math>."</p> </div> <div style="text-align: right;"> <p><math>120 \div 3</math></p> </div> <div style="background-color: orange; padding: 5px; margin-top: 10px;"> <p>New written methods can be modelled alongside mental or informal methods to ensure understanding.</p> </div>
<p>Representations to support written calculations</p>	<p>Use a range of concrete and pictorial resources, including:</p> <div style="display: flex; justify-content: space-between;"> <div style="border: 1px solid gray; padding: 5px;"> <p><math>98 \div 7 = 14</math></p> <p>Answer is 14</p> </div> <div style="border: 1px solid gray; border-radius: 50%; padding: 10px; text-align: center;"> <p><math>63 \div 3</math> equals three groups of 2 tens and a one.</p> </div> <div style="border: 1px solid gray; padding: 5px;"> <p><math>3 \overline{) 63} = 21</math></p> <p>I know that <math>63 \div 3 = 21</math>, so <math>63 \div 21 = 3</math>, and <math>21 \times 3 = 63</math>, so <math>3 \times 21 = 63</math>.</p> </div> <div style="border: 1px solid gray; padding: 5px;"> <p>An image for <math>56 \div 7</math></p> <p>The array is an image for division too</p> </div> </div> <div style="margin-top: 20px;"> <div style="border: 1px solid purple; border-radius: 15px; padding: 5px; display: inline-block;"> <p>How could I calculate <math>72 \div 3</math> ?</p> </div> <div style="border: 2px solid orange; padding: 10px; margin-left: 20px;"> <p>Informal exploration with manipulatives supports the progression to formal written methods—which is continued in Year 4.</p> </div> </div>



# Calculation policy

Written Calculations

Pupils practise and extend their use of the formal written methods of short multiplication and short division.

- Divide numbers up to 4 digits by a one-digit number using the formal written method of short division and interpret remainders appropriately for the context.

98 ÷ 7 becomes

$$\begin{array}{r} 14 \\ 7 \overline{) 98} \\ \underline{7} \phantom{0} \\ 28 \\ \underline{28} \\ 0 \end{array}$$

Answer: 14

432 ÷ 5 becomes

$$\begin{array}{r} 86 \text{ r}2 \\ 5 \overline{) 432} \\ \underline{40} \phantom{0} \\ 32 \\ \underline{30} \\ 2 \end{array}$$

Answer: 86 remainder 2

496 ÷ 11 becomes

$$\begin{array}{r} 45 \text{ r}1 \\ 11 \overline{) 496} \\ \underline{44} \phantom{0} \\ 56 \\ \underline{55} \\ 1 \end{array}$$

Answer: 45  $\frac{1}{11}$

- Pupils interpret non-integer answers to division by expressing results in different ways according to the context, including with remainders, as fractions, as decimals or by rounding. (See Representations below.)

**Revert to expanded methods if children find formal calculation method difficult**

Representations to support mental and written calculations.

Can we divide this token into 6 equal groups?, then we must exchange it for ten tokens. Can we divide into 6 groups now?

Short division with exchange.

$$\begin{array}{r} 23 \\ 6 \overline{) 138} \\ \underline{12} \phantom{0} \\ 18 \\ \underline{18} \\ 0 \end{array}$$

Hundreds	Tens	Ones
1	3	8

Practical experience with manipulatives is vital for children to talk through the language of division e.g. *exchange*, *remainder*; and to embed conceptual understanding.

Understanding remainders.

4

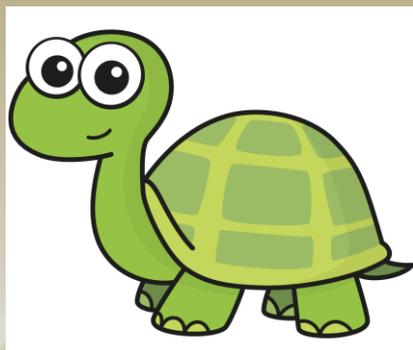
20	+	4	r. 2
10		10	
10		10	
10		10	
10		10	
10		10	
10		10	
10		10	
10		10	
10		10	

2 out of a whole group of 4 =  $\frac{2}{4} = \frac{1}{2} = 0.5$

$98 \div 4 = \frac{98}{4} = 24 \text{ r} 2 = 24\frac{1}{2} = 24.5$

What is the same? What's different about the ways that these remainders are expressed?

# Why is using precise mathematical language so important?



“Use of precise mathematical language enables all pupils to communicate their reasoning and thinking effectively. If a pupil fails to grasp a concept or procedure, this is identified quickly, and gaps in understanding are addressed systematically to prevent them falling behind.”

NCETM

**I think Tiny is correct/incorrect because...**

**If I know... then I know...**

**I agree/disagree because...**

**I think this is always/sometimes/never true because...**

**I noticed that...**





# Mathematical language

addition sign

is equivalent to

$$9 + 5 = 14$$

addend

addend

sum

**Addition** (commutative)



# Mathematical language

minus sign is equivalent to

$$7 - 4 = 3$$

minuend

subtrahend

difference

## Subtraction



# Mathematical language

multiplication sign is equivalent to

$$4 \times 5 = 20$$

factor

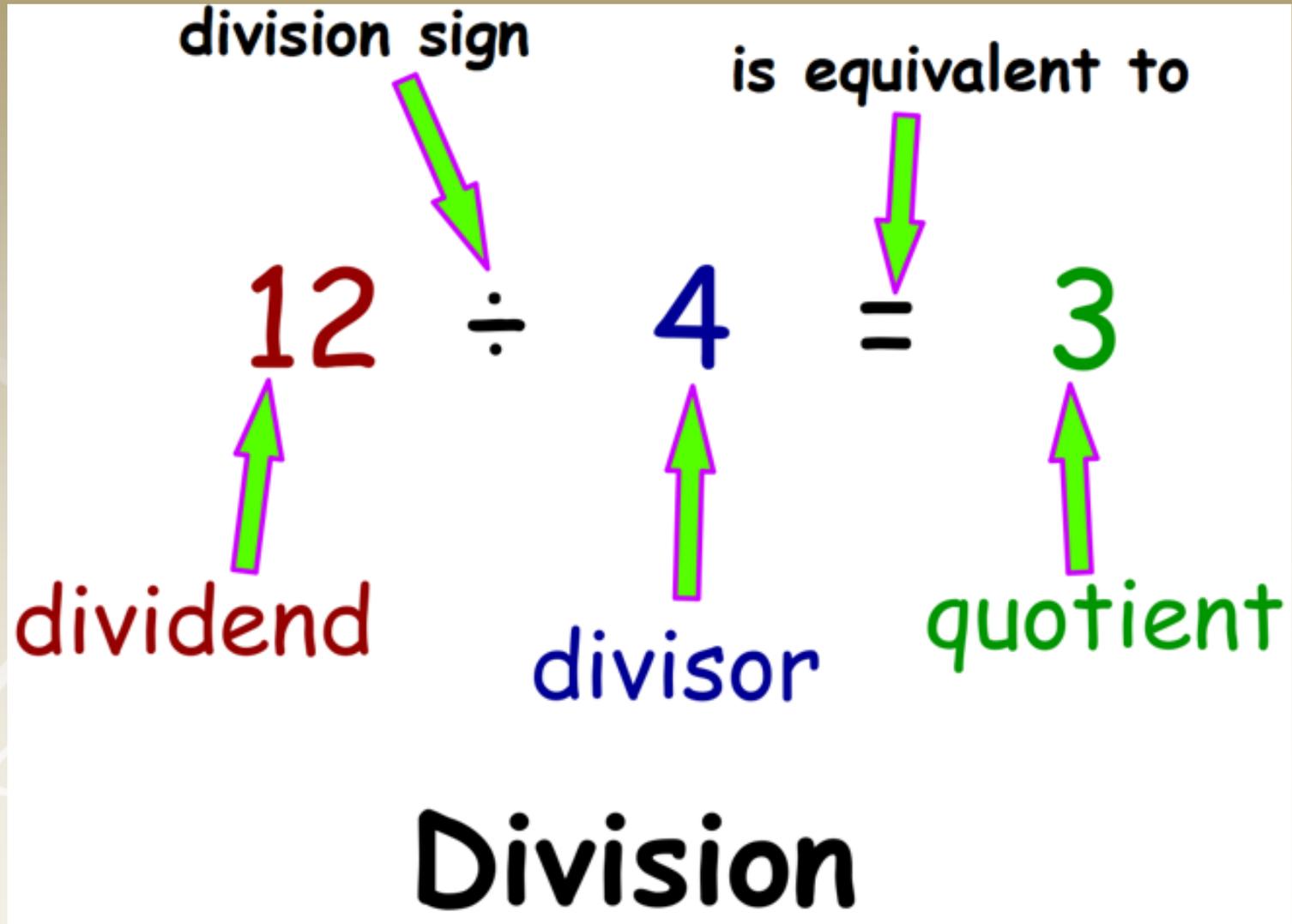
factor

product

**Multiplication** (commutative)



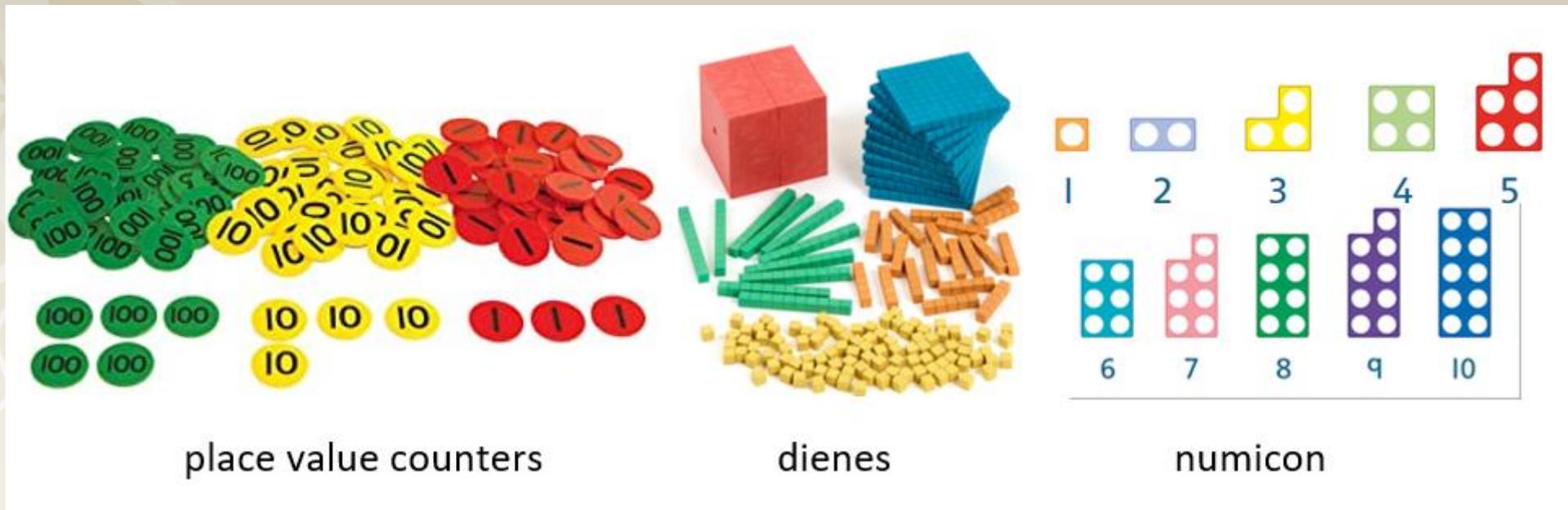
# Mathematical language



# Practical resources and visual representations



“Unlike traditional maths teaching methods where teachers demonstrate how to solve a problem, the CPA approach brings concepts to life by allowing children to experience and handle physical (concrete) objects.”  
Maths, No Problem!



place value counters

dienes

numicon